

Appendix D: EQUATIONS OF MOTION

There are 4 equations which can be used whenever an object travels with **constant, uniform acceleration** in a straight line.

We write these equations using 5 symbols:

s = distance traveled (in meters)

u = initial velocity (in meters per second)

v = final velocity (in meters per second)

a = acceleration (in meters per second squared)

t = time taken (in seconds)

Suppose an object is travelling at a velocity u and then moves with a uniform acceleration a for a time t . Its velocity is then v and it has traveled a distance s .

Next to the equation given below, interpret what it means in your own words:

$$v = u + at$$

$$s = \frac{(u + v)}{2} t$$

$$s = ut + \frac{1}{2} at^2$$

$$v^2 = u^2 + 2as$$

Rearrange the formulas above to make the letters in brackets the subject of the formula. Record the solution from the TI-92. Determine if your result is equivalent to the one given by the TI-92, explaining fully. Show your working out. If it is not equivalent, attempt the problem again.

1. $v = u + at, [a, t, u]$

2. $s = \frac{u + v}{2} t, [u, v, t]$

3. $s = ut + \frac{1}{2} at^2, [a, t, u]$

4. $v^2 = u^2 + 2as, [u, a, s]$

For the following problems, use the appropriate formula from the original four or those you rearranged to solve them.

1. A sports car accelerates from rest at 4 meters per second squared for 10 seconds. Calculate the final velocity.
2. A cheetah starts from rest, and accelerates at 2 meters per second squared for 10 seconds. Calculate:
(a) the final velocity and (b) the distance traveled.
3. A ball is thrown vertically upwards at 20 m/s. Ignoring air resistance and taking a to be the acceleration due to gravity (about 10 meters per second squared), calculate:
(a) how high it goes, (b) the time taken to reach this height, and (c) the time taken to return to its starting point.
4. A car with a crash-test dummy is travelling down a test track at a speed of 13 m/s. When the car hits the brick wall at the end of the track, it is as if it fell from the top of a house. Find the height of the house. (Use $a = 10 \text{ m/s}^2$, the acceleration of free fall.)

The examples above were taken from:

Johnson, Keith [1996], Physics for You, Stanley Thornes (Publishers) Ltd, pages 133, 139.